

**LARSON—INFO 790—CLASSROOM WORKSHEET 03**  
**Using CONJECTURING on CoCalc**

1. Log in to CoCalc.
  - (a) Start the Chrome browser.
  - (b) Go to `https://cocalc.com`
  - (c) Login (**your VCU email address** is probably your username).
  - (d) You should see an existing Project for our class. Click on that.
  - (e) Click “New”, then type **790-c03** into the box, and click “Jupyter Notebook”.
  - (f) When your notebook opens look on the upper-right to make sure the SageMath kernel is running.
  
2. Load “conjecturing.py” by running `load("conjecturing.py")`. (Your “790-c03.ipynb” must be in your Home/root directory for this to work, and there should be an “expressions” and “conjecturing.py” file there too).

### Conjecturing Properties

3. Try this first simple example. Interpret the conjectures. Are they true?

```
objects = [2,3,4]
properties = [Integer.is_prime, Integer.is_square, Integer.is_squarefree]
property_of_interest = properties.index(Integer.is_prime)
propertyBasedConjecture(objects, properties, property_of_interest,
    sufficient=True)
```

4. How does the *Truth* heuristic work in the “properties” case?
5. How does the *Significance* heuristic work in the “properties” case?
6. Re-run the code to see some under-the-hood details using the *verbose* and *debug* options:

```
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properties = [Integer.is_prime, Integer.is_square, Integer.is_squarefree]
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propertyBasedConjecture(objects, properties, property_of_interest,
    sufficient=True, debug=True, verbose=True)
```

## Gravity Example

In the paper you read this week, one of the examples was about using the CONJECTURING program for how Newton's Law of Gravitation ( $F = g \frac{m_1 m_2}{r^2}$ , where  $m_1$  and  $m_2$  are the masses of two bodies,  $r$  is the distance between them,  $g$  is the gravitational constant, and  $F$  is the force between the bodies). We can run this experiment ourselves.

7. Copy the file "gravity\_example.sage" from your Handouts folder to your Project's Home/root directory.
  8. We will shortly run that script. Open that file first (by clicking on "gravity\_example.sage" from your Home directory file list) and we'll talk about the code.
  9. Find the call to the `Conjecturing` program. What are the *objects*? What is their *type*? What are the *methods* available for those objects?
  10. How can we get an example of one of the objects? (Let `example = train_pairs[0]`).
  11. In your worksheet, run `load("gravity_example.sage")`. You should get a number of conjectures. Do you see anything that looks like Newton's Law?
  12. How can we get an example of one of the conjectures? (Let `conj = pair_above_conjs[0]`).
  13. How can we evaluate conjecture `conj` for our *example*? (Run: `conj.evaluate(example)`). This will be `TRUE` or `FALSE` depending on whether the example is true for the conjectured bound.
- Later we'll see that these *invariant conjectures* (which are in fact properties) can be used as properties for property conjectures (they will give us new novel properties besides properties/booleans/classes that are given with a specific problem).
14. What is we want just the *value* the conjectured bound gives for a specific object? (Run: `conj[0].evaluate(example, returnBoundValue=True)`).