Last name _____

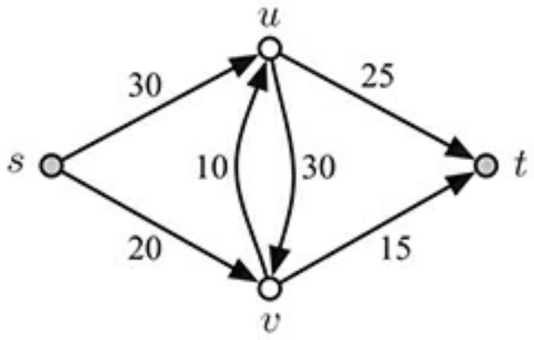
First name _____

LARSON—OPER 731—CLASSROOM WORKSHEET 22
Farkas's Lemma!

Concepts

- (Sec. 3.1) *dual LP*, *Weak duality theorem.*
- (Sec. 4.3) *complementary slackness*, cone, *cone of tight constraints.*
- (Sec. 4.4) *Farkas Lemma.*
- (Sec. 5.1) *primal-dual algorithm.*
- (Sec. 5.3) *directed graph*, *flow*, *flow balance*, *flow value*, *capacity*, *max-flow min-cut.*

1. What is *Farkas's Lemma*?

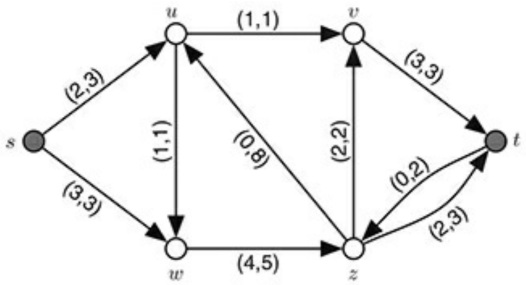


2. What is a *directed graph*?

3. What is an *s-t flow*? What is the *value* of a flow?

$$f_x(q) := \sum(x_a : a \in \delta^+(q)) - \sum(x_a : a \in \delta^-(q)) = 0,$$

4. What does the notation in the *flow balance* equation mean?



5. The first numbers on each edge are flow values and the second numbers are edge capacities. Do the flow values indicate a valid flow? What is the value of this flow?

6. Can you find a flow with a larger value in this network? If not, can you prove that this flow is maximum?

7. Model the maximum s-t flow problem for this network.

8. What is an *s-t cut*? What is the *capacity* of an s-t cut?

9. Can you find a minimum cut in this network?