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First name _____

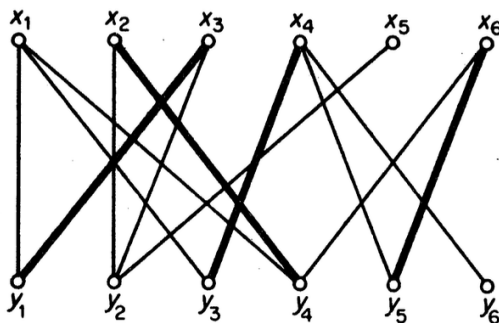
LARSON—MATH 556—CLASSROOM WORKSHEET 12
Berge's Theorem and the Hungarian Method

Concepts & Notation

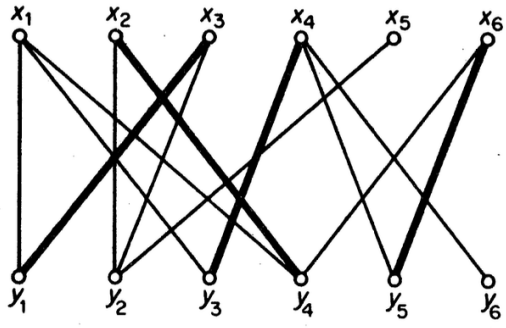
- *assignment problem, graph G , points $V(G)$, lines $E(G)$, adjacent, incident.*
- *line covering, line covering number ρ , matching, matching number ν , point covering, point covering number τ , independent set, independence number α .*

Review

- **König's Theorem:** For any bipartite graph, $\tau = \nu$.
- Let M be a matching in a graph. What is an M -alternating path?
- Let M be a matching in a graph. What is an M -augmenting path?

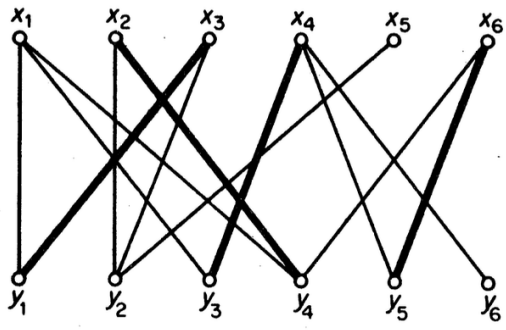


1. Let M be the highlighted lines. Find an M -augmenting path in this graph.

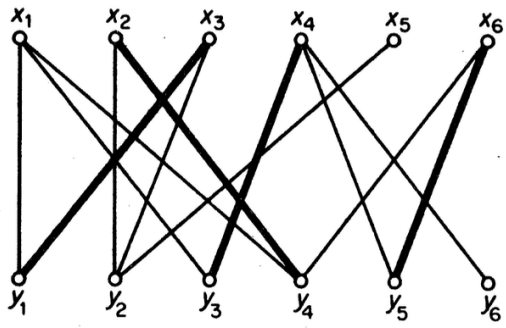


2. What is Berge's Theorem?

3. Why is Berge's Theorem true?



4. What is the *Hungarian Method*?



5. Why does the Hungarian method produce a *provably* maximum matching in a bipartite graph?