Last name
First name
LARSON—MATH 353–CLASSROOM WORKSHEET 21 Multiplicative Functions & Primitive Roots.
Review
1. (Theorem 2.2.2, Chinese Remainder Theorem). Let $a,b\in\mathbb{Z}$ and $n,m\in\mathbb{N}$ such that $\gcd(n,m)=1$ . Then there exists $x\in\mathbb{Z}$ such that
$x \equiv a \mod m$ ,
$x \equiv b \mod n$ .
Moreover $x$ is unique modulo $mn$ .
Multiplicative functions
1. What is a multiplicative function?
2. Is Euler's $\phi$ function multiplicative?

## **Primitive Roots**

3. We proved that, if an integer p is prime, then  $\mathbb{Z}/p\mathbb{Z}$  is a field. If an integer n > 1 is not prime, can  $\mathbb{Z}/n\mathbb{Z}$  be a field?

4. What is a *primitive root* in  $\mathbb{Z}/n\mathbb{Z}$  (for integer n > 1)?

