

First name _____

1. What is the Division Algorithm? (How can we *find* q and r)?
2. Why does **Lemma 1.1.10** imply that, for $a, b > 0$, with unique integers q, r with $a = bq + r$ ($0 \leq r < b$), that $\gcd(a, b) = \gcd(b, r)$?
3. How can the Division Algorithm be used to compute $\gcd(a, b)$?

4. Use the division algorithm repeatedly to compute $\gcd(2261, 1275)$.

(Theorem 1.1.19. Euclid). Let p be a prime and $a, b \in \mathbb{N}$. If $p|ab$ then $p|a$ or $p|b$.

5. Why is Euclid's Lemma true?

(Proposition 1.1.20) Every natural number is a product of primes.

6. Why is Proposition 1.1.20 true?

7. What is the Fundamental Theorem of Arithmetic?

8. How can we use Euclid's Lemma to prove the Fundamental Theorem of Arithmetic?