

Last name \_\_\_\_\_

First name \_\_\_\_\_

LARSON—MATH 350—CLASSROOM WORKSHEET 14  
Pascal's Triangle!

Review

- What is the *Binomial Theorem*?
  - What is *Pascal's Triangle*? Why does the  $i^{\text{th}}$  row sum to  $2^i$ ? Why are the “outside” terms all equal to 1? does does each “inside” term equal the sum of the two terms above it?
1. Draw 9 layers of Pascal's Triangle. Next to it, draw a second triangle with the values of the coefficients from Pascal's Triangle.

2. What formula did we conjecture for of the squares of the numbers in a layer of Pascal's triangle?
3. Can you prove it?

### **Fibonacci Numbers!**

4. A staircase has 2 steps. You take 1 or 2 steps at a time. How many ways are there to go up the steps?
5. A staircase has 3 steps. You take 1 or 2 steps at a time. How many ways are there to go up the steps?
6. A staircase has 4 steps. You take 1 or 2 steps at a time. How many ways are there to go up the steps?
7. A staircase has  $n$  steps. You take 1 or 2 steps at a time. How many ways are there to go up the steps?
8. How is the *Fibonacci sequence*  $F_n$  ( $n \geq 0$ ) defined?
9. Write out the terms  $F_0$  through  $F_{10}$ .